



CANBERRA SECONDARY SCHOOL



2024 Preliminary Examination

Secondary Four Express/Five Normal Academic

MATHEMATICS

4052/01

20 Aug 2024

2 hours 15 minutes

1130h – 1345h

Name: _____ () Class: _____

READ THESE INSTRUCTIONS FIRST

Write your full name, class and index number on all work you hand in.

Write in dark blue or black pen on both sides of the paper.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** the questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

Calculators should be used where appropriate.

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For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 90.

FOR MARKER'S USE		
	Marks Awarded	Max Marks
Total		90

This question paper consists of 21 printed pages including the cover page.

Setter: Mr Ng Chuen Joo

Mathematical Formulae

Compound interest

$$\text{Total amount} = P \left(1 + \frac{r}{100} \right)^n$$

Mensuration

$$\text{Curved Surface area of a cone} = \pi r l$$

$$\text{Curved surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector Area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f} \right)^2}$$

Answer **all** the questions.

1 Solve $9 - \frac{1}{2}x = 25$.

Answer $x =$ [1]

- 2 Ahmad, Simon and Bala share a sum of money in the ratio 3 : 2 : 5.
If Bala has \$900 more than Simon, what is the sum of money being shared by the three of them?

Answer \$ [2]

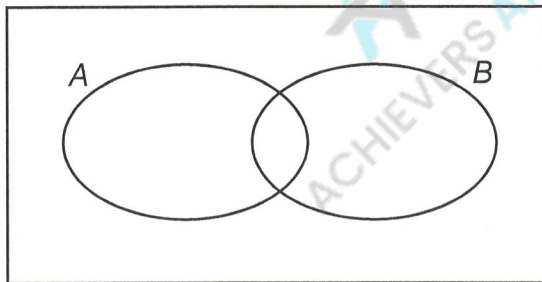
3 Write as a single fraction in its simplest form $\frac{3}{2a-1} - \frac{2}{1-2a}$.

Answer [2]

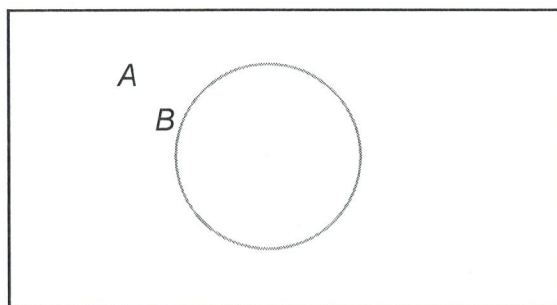
- 4 Five positive integers have a mean of 5, median of 4, mode of 3 and a range of 7. Find the five numbers.

Answer [2]

- 5 (a) On the Venn diagram, shade the region that represents $A' \cup B$. [1]



- (b) Use set notation to describe the shaded region.



Answer [1]

- 6 The quadratic curve can be written as .
 (a) Find the value of a and the value of b , where a and b are positive integers.

Answer $a =$ [1]

$b =$ [1]

- (b) Explain why y will not have a value smaller than -25 .

Answer

.....
 [1]

- 7 (a) Expand and simplify $(3x - y)(y + x)$.

Answer [2]

- (b) Factorise completely $3 - 12a^2$.

Answer [2]

- 8 (a) Given that _____, find the value of x .

Answer [1]

- (b) Simplify $4 \div \left(\frac{x}{2}\right)^{-2}$, giving your answer in positive index.

Answer [2]

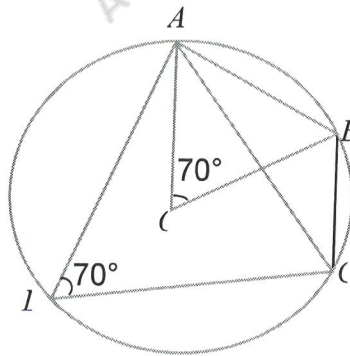
-
- 9 (a) $x^2 - 10x + 27$ can be expressed in the form $(x + p)^2 + q$.
Find the value of p and the value of q .

Answer $p =$ [1]

$q =$ [1]

- (b) Hence write down the coordinates of the minimum point of the graph of $y = x^2 - 10x + 27$.

Answer (.....,) [1]



In the diagram, O is the centre of the circle and $ABCD$ is a cyclic quadrilateral.

Angle $AOB = \text{angle } ADC = 70^\circ$.

Explain why triangle ABC is an isosceles triangle.

Give reasons for each step of your working.

[3]

- 11 (a) The angles of a quadrilateral taken in order are $3x$, $6x$, $5x$ and $4x$. Find the value of x .

Answer $x =$ [1]

- (b) Explain whether the quadrilateral is a parallelogram or a trapezium.

..... because [2]

- 12 A square pyramid P has base with side x m, height y m and a volume of 300

Find

- (a) the volume of a similar square pyramid, which has a height double that of the pyramid P .

Answer

[1]

- (b) the volume of another square pyramid with side $3x$ m and height y m.

Answer

[2]

- 13 The following stem-and-leaf diagram shows the scores of students in a math test.

Stem	Leaf
6	8 9
7	0 2 3 3 4 4 4 7 8
8	3 4 5 6 7 7 9
9	1 3 7

6|8 represents 68 marks

Find

- (a) the median score,

Answer

[1]

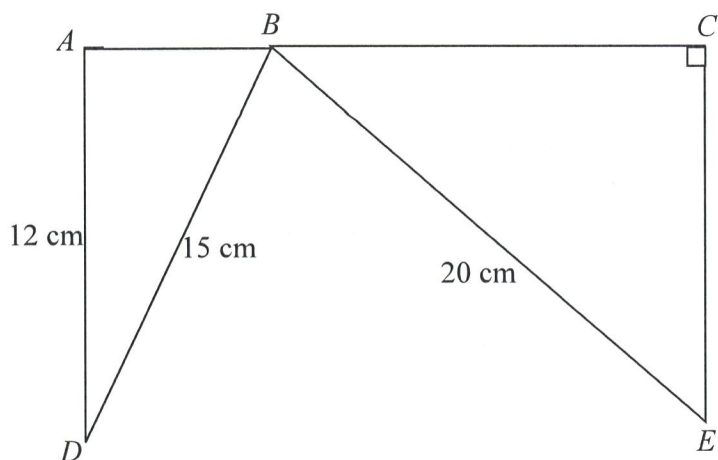
- (b) the interquartile range.

Answer

[2]

- 14 In the diagram, there are two right-angled triangles $\triangle ABD$ and $\triangle CEB$ such that

$AD = 12$ cm, $BD = 15$ cm and $BE = 20$ cm.



- (a) Find $\cos \angle ABD$.

Answer [2]

- (b) If $\triangle ABD$ and $\triangle CEB$ are similar, find the length of BC .

Answer cm [2]

- 15 As of 2023, the population of Singapore is approximately 5.64 million and the population of Malaysia is approximately 33.57 million.

- (a) Find the total population of both countries, giving your answer in standard form.

Answer [2] [2]

- (b) The population of Singapore in 2023 was 5% more than its population in 2013.
Calculate the population of Singapore in 2013.

Answer [2]

- 16 A box contains 15 marbles of which x are green and the rest are yellow.

- (a) Write down the probability, in terms of x , that a marble chosen from the box is yellow.

Answer [1]

- (b) When 5 more green marbles are added to the box, the probability of choosing a yellow marble becomes $\frac{1}{2}$.
Find the initial number of green marbles in the box.

]

Answer

[2]

- 17 (a) (i) Express 1500 as the product of its prime factors.
Leave your answer in index notations.

[Turn Over]

Answer [1]

- (ii) $p = 2^m \times 3^2 \times n$, where m and n are positive integers.
Find the values of m and n if the HCF of 1500 and p is 6,
given that $100 < p < 150$.

Answer $m =$ [1] $n =$ [1]

- (b) In a race, Car A, Car B and Car C took 3 minutes, 6 minutes and 8 minutes respectively to complete one lap around the racing track.
If the race started at 7 pm, at what time will the cars be back at the starting point together again?

Answer

[1] [2]

- 18 A length of 5 cm on a map represents an actual distance of 2.5 km.

Find

- (a) the actual distance represented by 20 cm on the map, giving your answer in km,

Answer

km [1] [1]

- (b) the scale of the map in the form 1 : n ,

Answer

km [2]

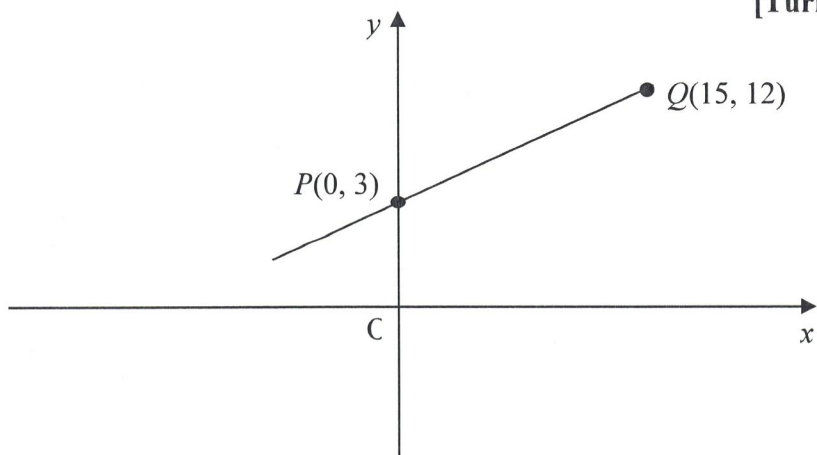
- (c) the land area in , which is represented by on the map.

Answer

km [2]

- 19 The coordinates of P and Q are $(0, 3)$ and $(15, 12)$ respectively.

[Turn Over]



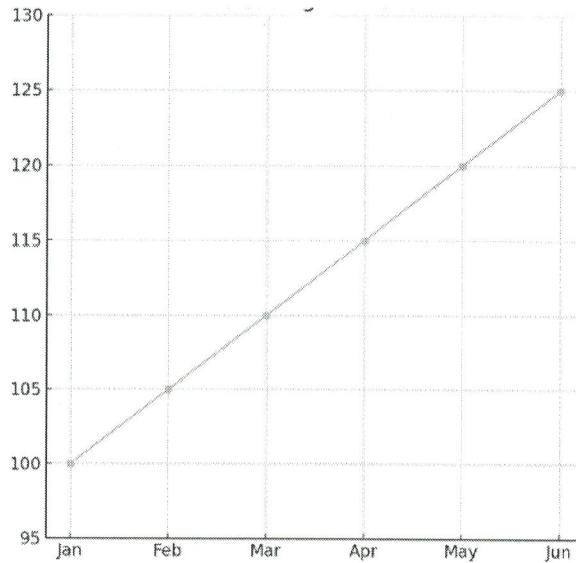
- (a) Find the equation of PQ .

Answer [2]

- (b) Find the perimeter of trapezium $OPQR$, where O is the origin and R is the point of reflection of Q along the x -axis.

Answer [3]

- 20 The line chart below shows the sales performance of a company.



Explain what is misleading about this line chart and how it may mislead the reader.

.....

.....

..... [2]

- 21 12 men will take 54 days to complete a building project.

- (a) Assuming that the men work at the same rate, how long will it take for 9 men to complete the project?

Answer days [2] [1]

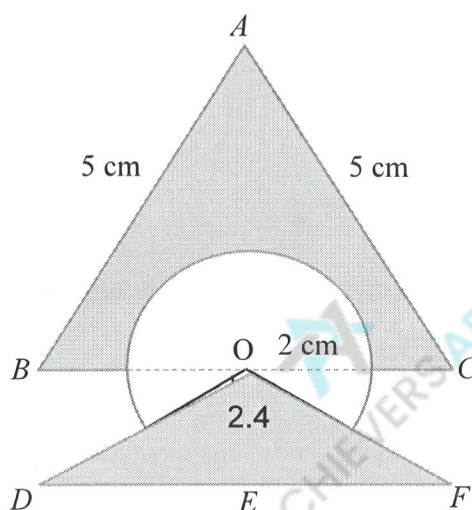
- (b) How many days can be saved if 6 more men are added to the team?

Answer

[
2days [2]
days

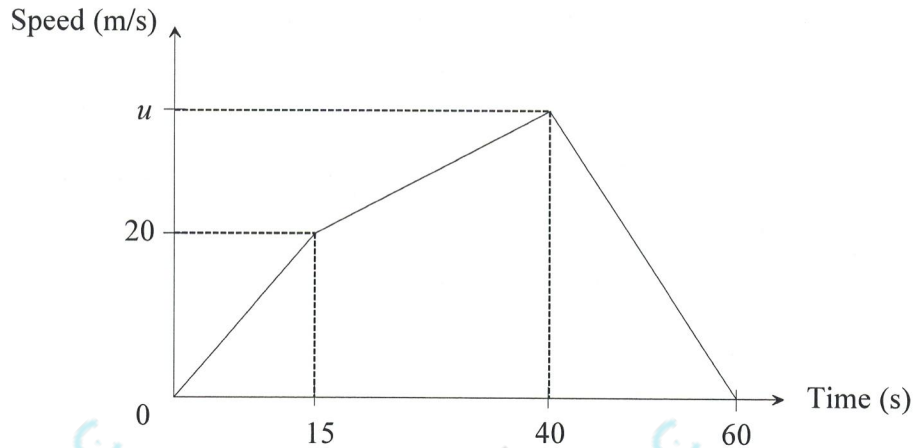
[Turn Over]

- 22 A logo, as shown below, has a circle with centre O and radius 2 cm, an equilateral triangle ABC of side 5 cm and an isosceles triangle ODF with $OD = OF$.
 DEF is a tangent to the circle at E and angle $DOF = 2.4$ radians.
 Half of the circle lies inside triangle ABC .
 Calculate the area of the shaded region.



Answer cm^2 [5]

- 23 The diagram below shows the speed-time graph of a car which starts from rest.



- (a) Calculate the speed of the car after 9 seconds.

Answer m/s [2]

- (b) (i) Find the value of u , if the total distance covered in the first 40 seconds is 900 m.

Answer [2]

- (ii) Hence find the deceleration of the car at the last 20s.

Answer

[1]

- 24** At Café A, a latte costs \$3.50, a croissant costs \$2.70 and a sandwich costs \$5.00. At Café B, a latte costs \$0.40 more, a croissant costs \$0.20 less and a sandwich costs \$0.50 less.

[Turn Over]

This information can be represented by the matrix $Q = \begin{pmatrix} 3.50 & 0.40 \\ 2.70 & -0.20 \\ 5.00 & -0.50 \end{pmatrix}$.

- (a) Azza buys 2 latte, 3 croissants and 3 sandwiches.
Yu Fei buys 1 latte and 4 sandwiches.
Represent their purchases in a 2×3 matrix P .

Answer $P =$

$$\begin{pmatrix} & & \\ & & \end{pmatrix}$$

[1]

- (b) Evaluate $M = PQ$.

Answer $M =$

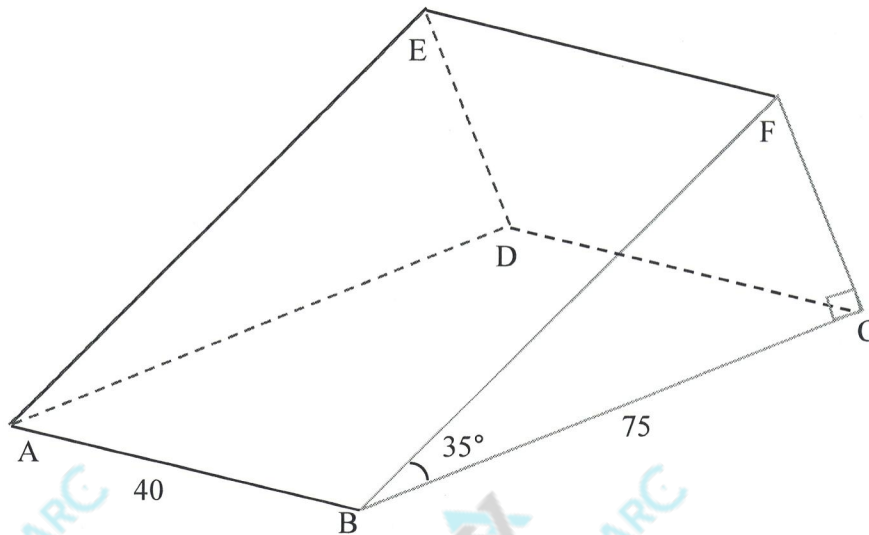
$$\begin{pmatrix} & \\ & \end{pmatrix}$$

[2]

(c) Should Azza buy from Café A or Café B? Give your reasons.

[2]

25



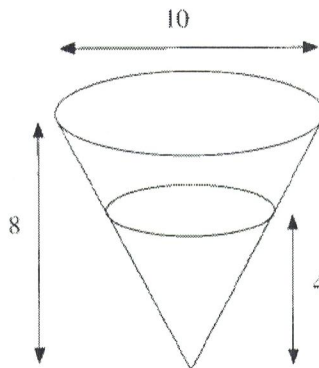
In the diagram, a wooden ramp is shown where $\angle BCF = 90^\circ$ and $\angle CBF = 35^\circ$. $ABCD$, $CDEF$ and $ABFE$ are rectangles. $AB = 40$ cm and $BC = 75$ cm. Find $\angle FAC$.

26

A conical container with a diameter of 10 cm and a height of 8 cm is filled with water to a depth of 4 cm.

Answer [3]

[Turn Over]



- (a) Show that the volume of the water in the container is $\frac{25}{3}\pi \text{ cm}^3$.

[2]

- (b) Find the surface area of the inside of the container that is in contact with the water.

Answer cm² [2]

- (c) The water in the cone is poured into a test tube.
The test tube is made by joining together a cylinder of diameter 3 cm and a hemisphere of diameter 3 cm.
Calculate the height of the water in the test tube.



Answer cm [3]

End of paper



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MATHEMATICS

4052/02

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Setter: Ms Sim Yi Lian

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Answer **all** the questions.

- 1 (a) Solve the simultaneous equations.

$$4m + 6n = 58$$

$$3m + 5n = 46$$

Answer $m =$

$n =$ [3]

- (b) Write as a single fraction in the simplest form

Answer [3]

(c) $x = \sqrt[3]{\frac{25y}{7z+2}}$

- (i) Find x when $y = 25$ and $z = -1$.

Answer $x =$ [1]

- (ii) Rearrange the formula to make y the subject.

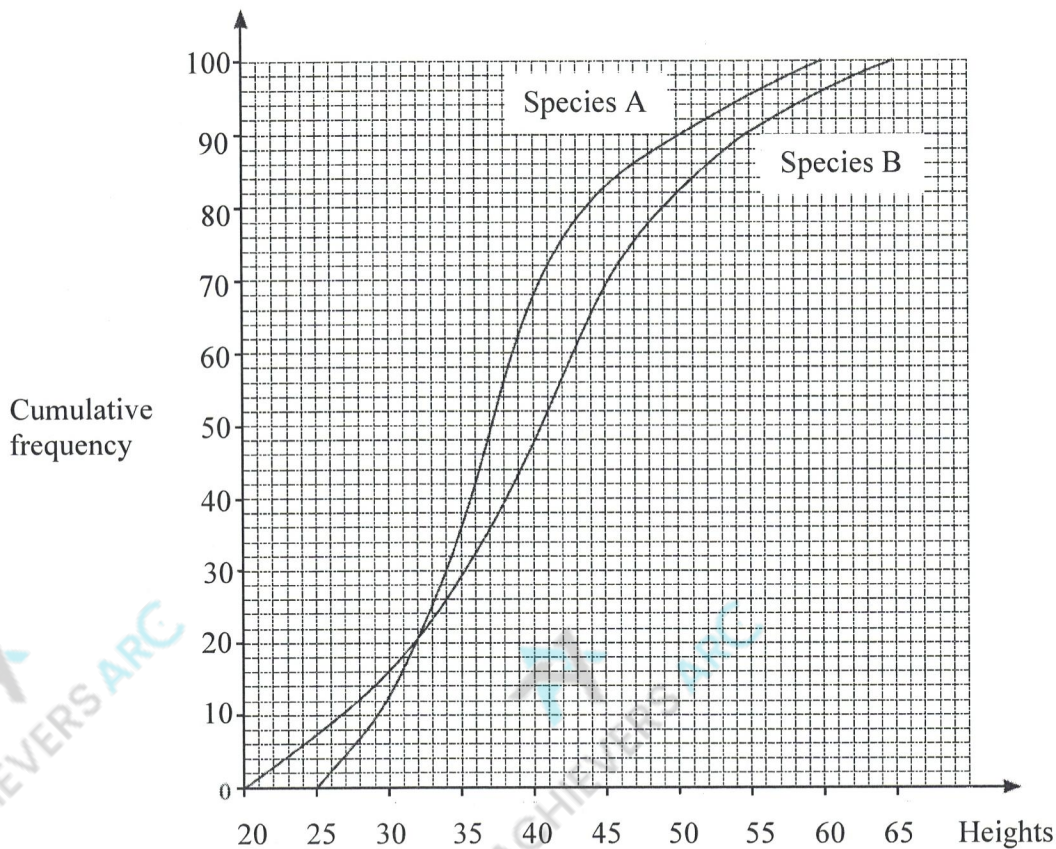
Answer $y =$ [2]

(d)

Solve the equation

Answer $x =$ or [3]

- 2 (a) The heights, in centimeters, of 100 plants of each of species A and species B are recorded.
The cumulative frequency curves show the distributions of their heights.



- (i) Use the curve to estimate
(a) the median height for species B,

Answer cm [1]

- (b) the 40th percentile for species A,

Answer cm [1]

- (c) the interquartile range for species A.

Answer cm [2]

- (ii) Plants from species B are used for an event.
Only plants with height within 10% of 50 cm are used.
Find the percentage of plants from species B which are used.

Answer % [2]

- (b) A box has 20 pots of plants.
There are 5 pink pots, 9 blue pots and the remaining pots are green.
- (i) Two pots are taken from the box at random, without replacement.
Find, as a fraction in its simplest form, the probability that one pot is pink and the other is blue.

Answer [2]

- (ii) These two pots are returned to the box.
Three pots are taken from the box at random, without replacement.
Find, as a fraction in its simplest form, the probability that only one pot is green.

Answer [2]

- 3 (a) Wayne inherited a sum of money from his parents.

He decided to invest 60% of the money and shares of the **remaining** amount with his wife.

The other \$20 000 are meant for their travelling expenses.

Calculate the sum of money he inherited.

Answer \$ [3]

- (b) A bank offers two investment packages.

Package A	Package B
<ul style="list-style-type: none"> • Simple interest of 0.97% per annum. • One time payout of 10% of the amount of the investment. 	<ul style="list-style-type: none"> • Compound interest of 3.78% per annum.

Wayne wants to invest \$55 000 in one of the packages for 3 years.

Which package should he choose if he wishes to reap the most benefits from the investment?

.....
 [5]

- (c) Wayne and his wife go on a seven days self-drive trip to Australia. They pay 150 AUD per day for car hire and 380 AUD per night for hotel. They pay using credit card and is charged with a fee of 2% for the currency conversion.
The exchange rate between Singapore dollars and Australian dollars is $\$1 = 0.91$ AUD.
Calculate the total amount, including credit card fee, Wayne is charged for car hire and accommodation.
Give your answer in Singapore dollars, correct to the nearest dollar.

Answer \$ [3]

- 10



- 

[2]

- similar to triangle QCF
 ment you make.

[2]

- (c) Diameter _____ cm and angle _____ .
Calculate the area of segment CD .

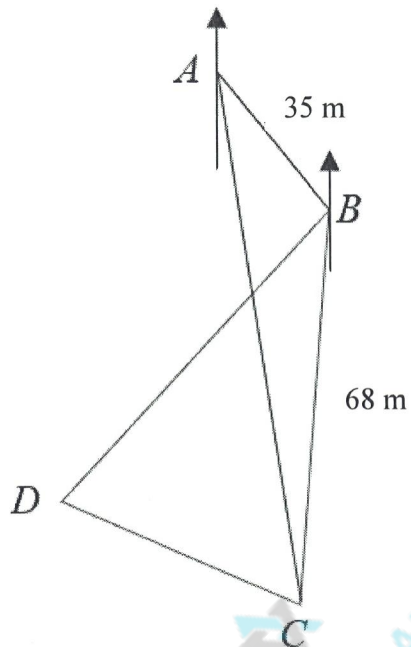
Answer cm^2 [4]

- 5 A, B, C and D are points on horizontal ground.

$AB = 35$ m and $BC = 68$ m.

The bearing of B from A is 137° and the bearing of C from B is 192° .

Angle $ACD = 125^\circ$ and angle $ADC = 105^\circ$.



- (a) Show that angle $ABC = 125^\circ$.

[2]

- (b) Calculate AC .

Answer m [3]

- (c) Calculate DC .

Answer m [2]

A man travels in a straight line from D to C .
 X , is the position of the man where it is the shortest distance from B during this journey.

- (d) Show that $BX = 63.9$ m.

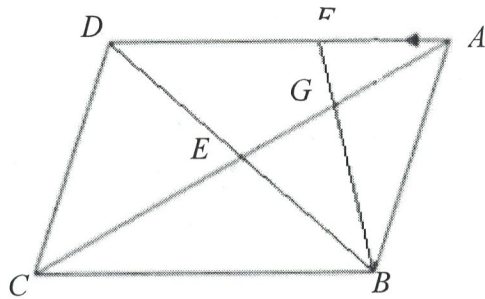
[2]

- (e) A drone is hovering vertically above B .
 The angle of elevation of the drone from C is 40.5° .
 Calculate the greatest angle of elevation of the drone from a point on DC .

Answer [3]

- (a) In the diagram $ABCD$ is a parallelogram.
The diagonal AC and BD intersect at E .

F is a point on AD such that
 G is the mid-point of AE .



- (a) Express \overrightarrow{DE} in terms of \mathbf{p} and \mathbf{q} , as simply as possible.

Answer [2]

- (b) Express \overrightarrow{AG} in terms of \mathbf{p} and \mathbf{q} , as simply as possible.

Answer [2]

(c) Show that

[2]

(d) Explain why B , G and F lie on a straight line.

.....

.....

.....

.....

[2]

(e) Calculate $\frac{\text{the area of triangle } ABF}{\text{the area of parallelogram } ABCD}$.

Answer [2]

7 (a)

Complete the table of values for

	0	1	2	3
0.25	3	2.75	1	1.75

[1]

(b) On the grid opposite, draw the graph of $y = \frac{x^3}{4} - 2x + 1$ for $-3 \leq x \leq 3$. [3]

(c) Explain how your graph shows that there is only one solution of the equation $\frac{x^3}{4} - 2x + 1 = k$ for some values of k .

..... [1]

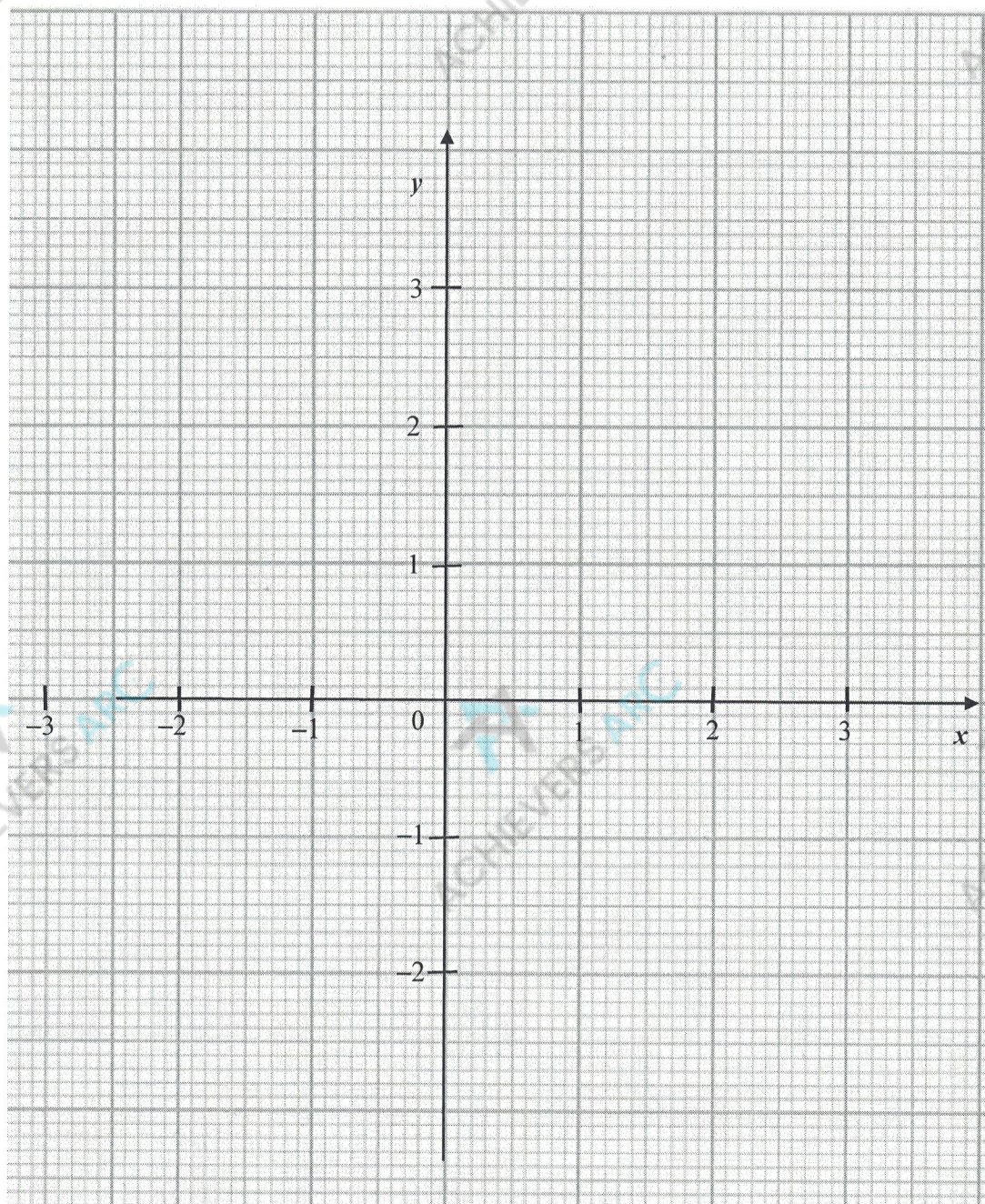
(d) The equation $x^3 - 9x - 4 = 0$ can be solved by drawing a suitable straight line on the grid.

(i) Find the equation of the straight line.

Answer [2]

(ii) By drawing this straight line, solve the equation $x^3 - 9x - 4 = 0$.

Answer $x =$ or [2]



- 8 The first four terms in a sequence of numbers are given below.

- (a) Find T_5 .

Answer [1]

- (b) Show that the n^{th} term of the sequence, T_n is given by $n^2 + 6n + 4$.

[2]

- (c) and T_p are consecutive terms in the sequence.

Find and simplify an expression, in terms of p , for the sum of and T_p .

Answer [3]

- (d) Find the value of p when the sum of T_{p-1} and T_p is 303.

Answer $p =$ [2]

- 9 Jim, his wife and their child visited Hokkaido, Japan.

The tables below give information that can be used to work out some of their expenses.

Payment mode	Prices of flight tickets for a return trip			
	Cash		Redemption with miles	
	(Includes tax)		(Excludes tax of \$115 per pax)	
Class	Economy	Business	Economy	Business
Adult	\$1920	\$5500	90 000 miles	140 000 miles
Child	\$1350	\$4000		

Amount of fuel used (litres/100 km)

Type of driving	Type of car		
	Sedan car	Sport Utility Vehicle (SUV)	Mini van
City	7.8	9.3	10.8
Out of city	5.7	7.5	8.9
Combined	6.2	8.8	9.5

Daily rates of driver

Day(s) of hire	8 hours	Additional time
1	\$350	\$45 per hour
2 or more	\$300	\$40 per hour

- (a) They travelled in business class and Jim had 150 000 miles to offset some of the cost of their flight tickets.
Calculate the amount of money he paid for the tickets.

Answer \$ [2]

- (b) Jim engaged a driver for 10 hours and his family travelled in a SUV for one day during their trip.
The driver picked them from their accommodation in the city to attractions outside the city.

The driver drove the first stage of the journey at an average speed of 70 km/h.

The second stage of the journey is 32 km longer than the second stage.

The driver drove at an average speed of 80 km/h.

The journey takes a total of 4 hours and 9 minutes.

Fuel price for the vehicle was \$1.70 per litre.

Jim paid \$550 to the driver.

He thinks that he included a 20% tips in the amount paid to the driver.

Is he correct?

Justify your decision with calculations.

[8]

End of paper

